

Lecture #15: Rollups

COMS 4995-001:
The Science of Blockchains
URL: <https://timroughgarden.org/s25/>

Tim Roughgarden

Bottlenecks to Scaling

Answer: load on validators.

- **consensus responsibilities:**
 - assembling a block (can be hard to do well, more later)
 - communication/bandwidth
 - computation (e.g., signature verification)

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- **storage responsibilities:**
 - storing sequence of all processed txs

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Approaches to Scaling

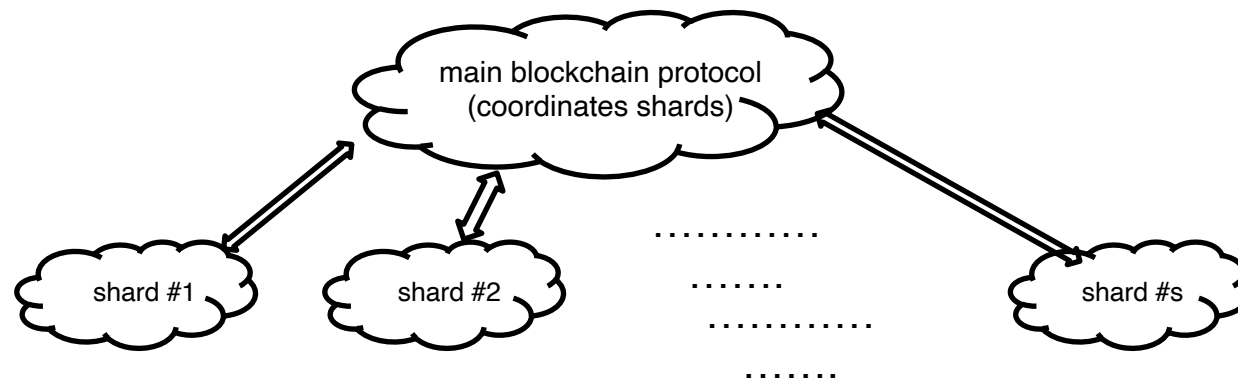
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Category #4: “sharding”/horizontal scaling.



Goals for Lecture #15

1. Introduction to “rollups.”

- an approach to sharding blockchain state and execution
- piggyback on an “L1” for data availability, liveness, etc.
- central to the Ethereum ecosystem

2. EIP-4844.

- modern solution to DA required by rollups: “blob” storage

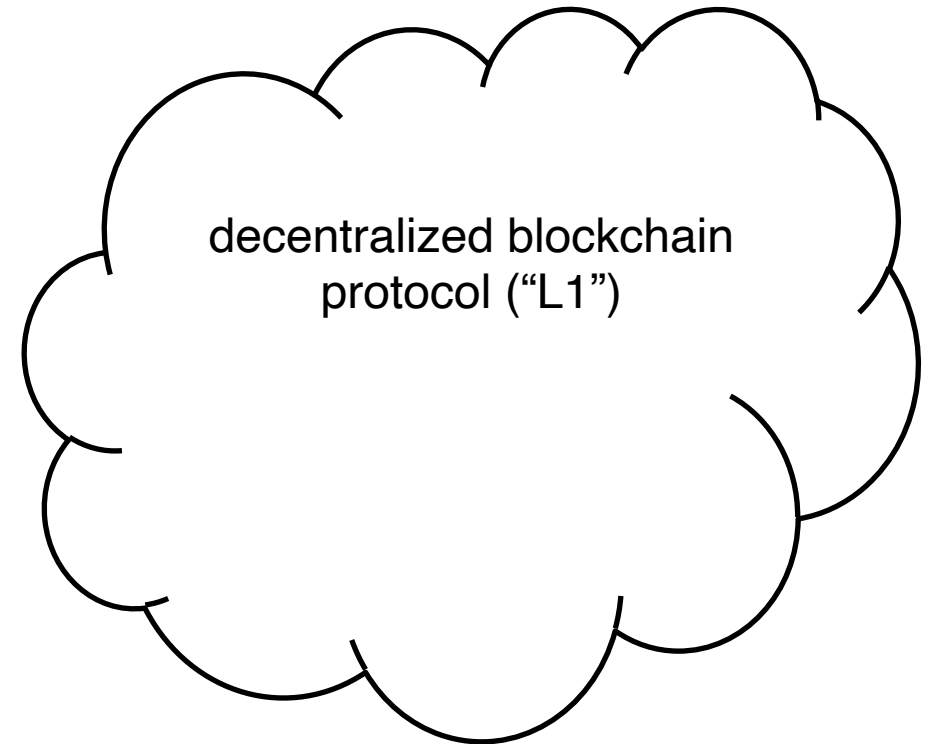
3. Optimistic rollups. (e.g., Arbitrum, Base, Optimism)

- rollup state commitments verified via “bisection game”
- security derived from economic penalties (confiscated collateral)

Introduction to Rollups

Assume: a decentralized “layer-one” blockchain (“L1”) with strong consistency and liveness guarantees. (e.g., Ethereum)

L1 ↔ Rollup Architecture



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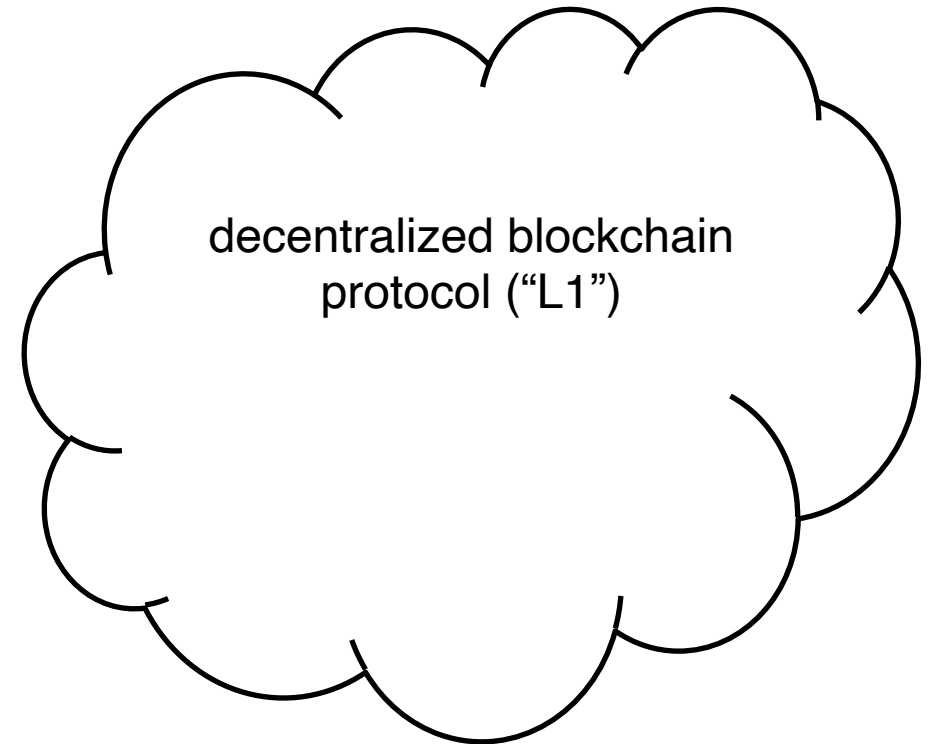
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- not necessarily decentralized, subject to crash or Byzantine failure
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(possibly centralized) rollup



decentralized blockchain
protocol ("L1")

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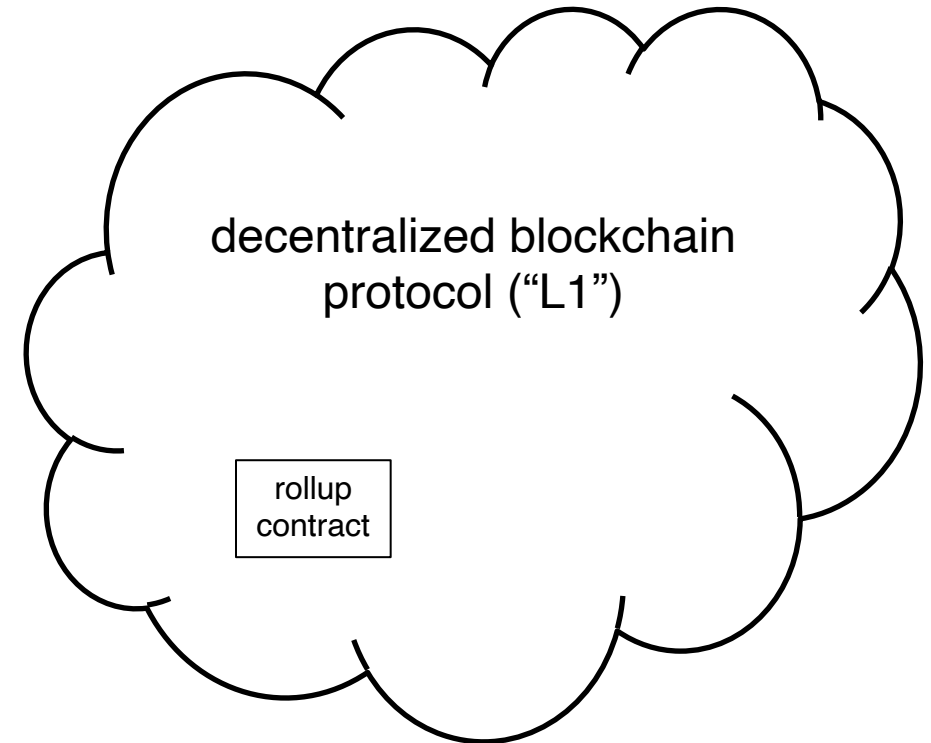
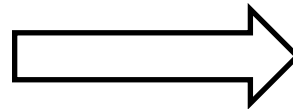
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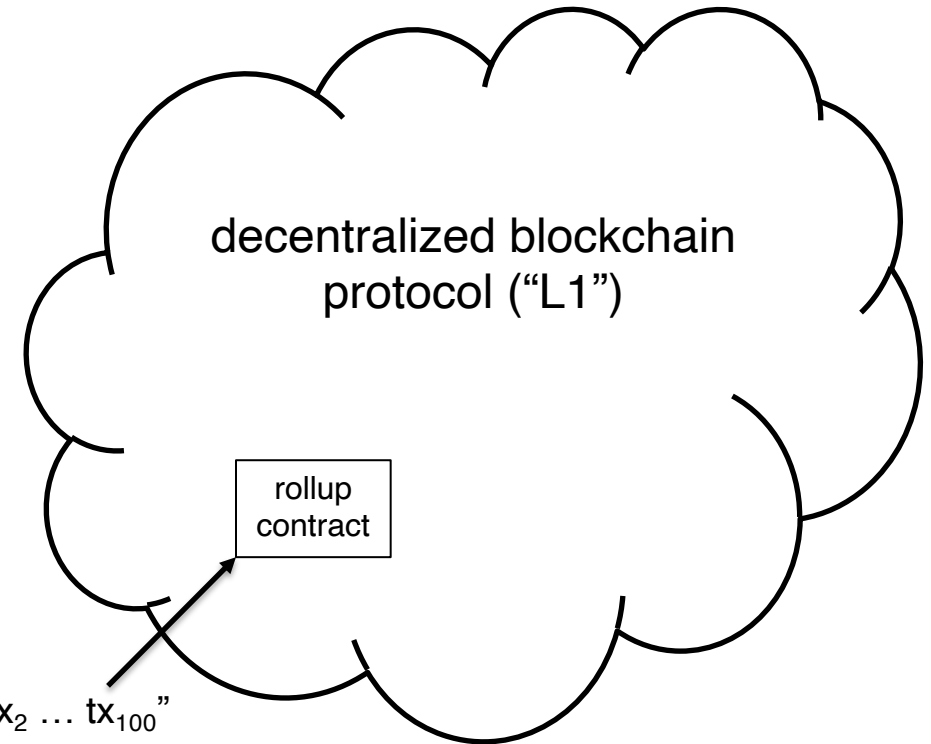
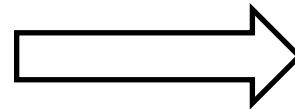
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- publishes rollup txs via L1 contract (i.e., uses L1 for data availability)
 - **note:** anyone can run a rollup full node (i.e., maintain full rollup state)

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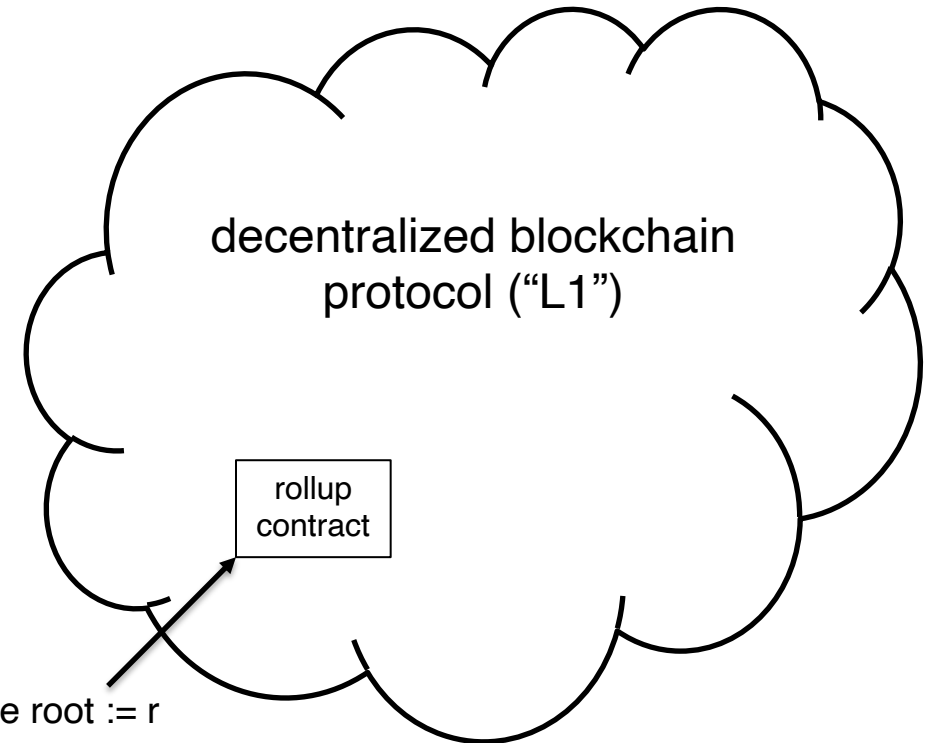
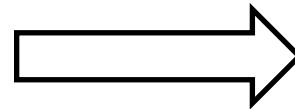
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 - **note:** anyone can run a rollup full node (i.e., maintain full rollup state)
 - periodically publishes commitment to rollup state (e.g. state root) to L1
 - **note:** any full node can check correctness of commitment

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Dealing with Rollup Failures

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Protection against rollup liveness failure: can “reboot” or “fork” rollup to resume execution from most recent state commitment.

- tx data available on L1 → blockchain state (not just state root) is known

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Protection against rollup safety failure: any full node can detect an incorrect state commitment and raise an alarm.

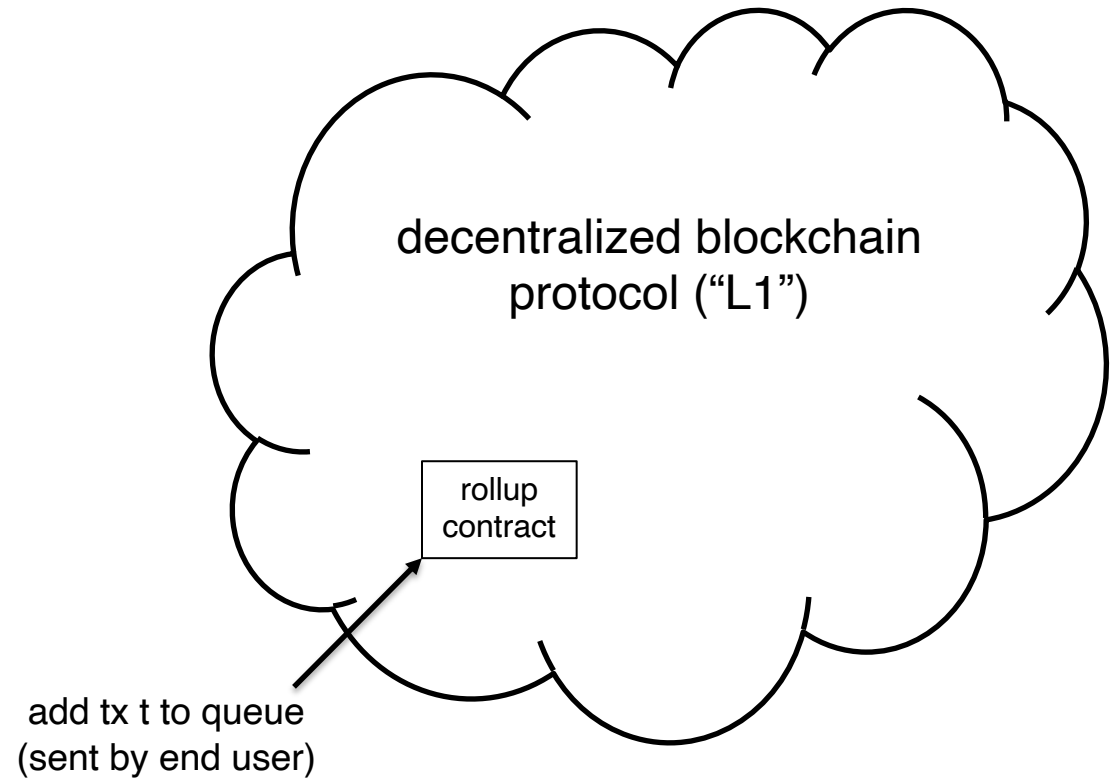
Two Requirements for “Classic” Rollups

1. **Escape hatch/forced tx inclusion via the L1.**
 - any user can send a rollup tx direct to the rollup’s L1 contract to force its inclusion in the next batch of rollup txs

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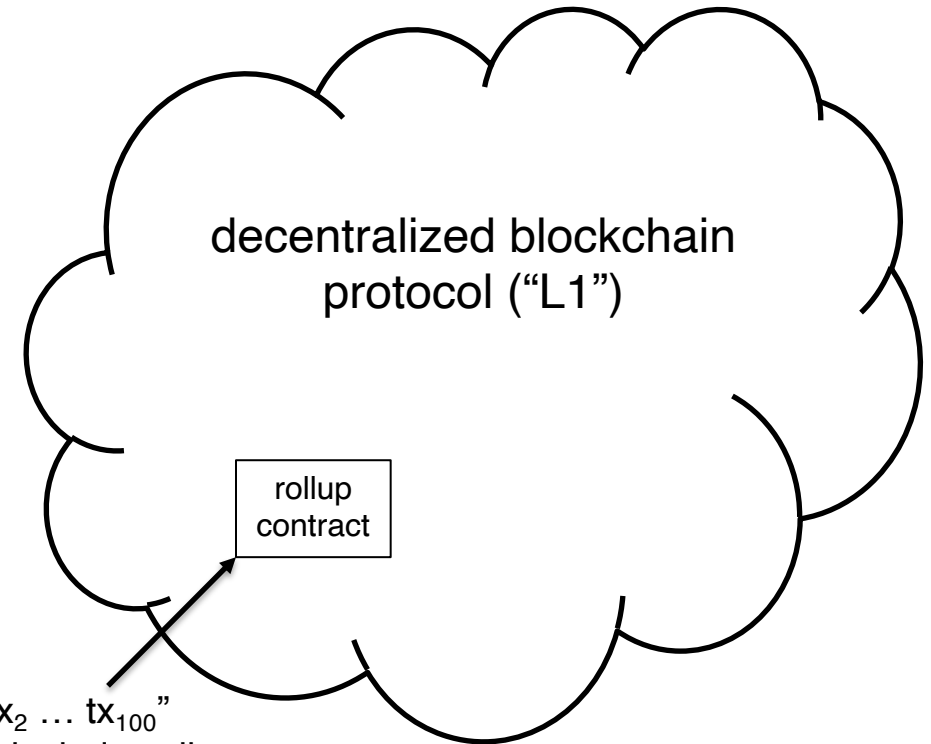
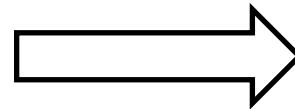
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 - L1 tx records the specified rollup tx in queue in rollup’s L1 contract
 - next publication of rollup txs must “clear the queue” to be valid

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publish "tx₁ tx₂ ... tx₁₀₀"
(invalid unless includes all txs in the contract's queue)

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Question: how can L1 verify correctness without tx re-execution?

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 - SNARKs known since mid-1990s, becoming practical in mid-2020s

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- economic guarantees (optimistic) vs. cryptographic guarantees (validity)
- common case requires little work (optimistic) vs. lots of work (validity)
- rollup txs might get reversed (optimistic) vs. final (validity)

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Upshot: rollup txs became much cheaper (by 10-100x).

- blobs priced separately from regular txs

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Dispute resolution: L1 contract determines correct commitment.

- **idea:** re-execute minimal amount to determine winner

Dispute Resolution

- Canonical scenario:** initial state commitment σ_0 , assumed correct.
- ordered batch $L = t_1, t_2, \dots, t_k$ of txs
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Bisection Games

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 - i.e., submits to rollup's L1 contract, which verifies the proof

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- if $\mu_{N/2} \neq \mu'_{N/2} \rightarrow$ recurse on first half of computation trace
- repeat until locate position i of computation s.t. $\mu_i = \mu'_i$ and $\mu_{i+1} \neq \mu'_{i+1}$

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Bisection game:

- sequencer, defender reveal midpoints $\mu_{N/2}, \mu'_{N/2}$ of computations
- repeatedly recurse on first or second half of computation trace until locate position i of computation s.t. $\mu_i = \mu'_i$ and $\mu_{i+1} \neq \mu'_{i+1}$

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- repeatedly recurse on first or second half of computation trace until locate position i of computation s.t. $\mu_i = \mu'_i$ and $\mu_{i+1} \neq \mu'_{i+1}$
- L1 contract directly verifies if transition $\mu_i \rightarrow \mu_{i+1}$ correctly computed

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Bisection game:

- sequencer, defender reveal midpoints $\mu_{N/2}, \mu'_{N/2}$ of computations
- repeatedly recurse on first or second half of computation trace until locate position i of computation s.t. $\mu_i = \mu'_i$ and $\mu_{i+1} \neq \mu'_{i+1}$
- L1 contract directly verifies if transition $\mu_i \rightarrow \mu_{i+1}$ correctly computed
 - \approx simulating one step of the EVM (inside a smart contract)
 - if not, contract rejects σ_1 as invalid, confiscates sequencer's stake
 - if so, contract confiscates challenger's stake

Properties of Optimistic Rollups

Resolving σ'_1 vs. σ_1 : view processing of txs in as a sequence of EVM states

- sequencer posts commitment r to its computation $\mu_1, \mu_2, \dots, \mu_N$
- defender posts commitment r' to its computation $\mu'_1, \mu'_2, \dots, \mu'_N$

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Good news: incorrect state commitment \rightarrow big economic penalty.

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Good news: incorrect state commitment → big economic penalty.

Bad news: requires time (days) for dispute resolution to play out.