Lecture #16: Optimistic Rollups

COMS 4995-001: The Science of Blockchains URL: https://timroughgarden.org/s25/

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### Goals for Lecture #16

- 1. Rollups review.
  - an approach to sharding blockchain state and execution
  - piggyback on an "L1" for data availability, liveness, etc.
  - central to the Ethereum ecosystem
- 2. Optimistic rollups. (e.g., Arbitrum, Base, Optimism)
  - rollup state commitments verified via "bisection game"
  - "cryptoeconomic" security: derived from economic penalties (confiscation of staked collateral)

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(possibly centralized) rollup



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  - pre-EIP-4844: via call data
  - post-EIP-4844: via blobs

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  - question: how can L1 do this without re-executing rollup txs itself?

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  - intuitively, a specific line of code that was executed incorrectly
- L1 verifies proof of incorrectness directly
  - L1 performs minimal re-execution necessary to resolve dispute
  - details quite complex, hard to get right

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Question: how can L1 know which state commitment is correct?

Idea: L1 performs minimal amount of re-execution necessary to determine winner (sequencer vs. challenger).

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**Canonical scenario:** initial state commitment  $\sigma_0$ , assumed correct.

- ordered batch  $L = t_1, t_2, \dots, t_k$  of rollup txs
- sequencer alleges that  $\sigma_1$  is correct state commitment after executing L
- challenger disagrees, posts alternative commitment  $\sigma'_1 \neq \sigma_1$
- for simplicity, suppose both L1 + rollup execution layers are EVM-based

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# Visualizing an EVM State



[source: https://www.quicknode.com/guides/ethereum-development/smart-contracts/a-dive-into-evm-architecture-and-opcodes]

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Throughout: if one party fails to submit expected L1 tx in a reasonable (TBA) amount of time  $\rightarrow$  lose dispute and its stake.

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- repeat until locate position i of computation s.t.  $\mu_i = \mu'_i$  and  $\mu_{i+1} \neq \mu'_{i+1}$

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  - ≈ simulating one step of the EVM (inside a smart contract)
  - if not, contract rejects  $\sigma_1$  as invalid, confiscates sequencer's stake
  - if so, contract confiscates challenger's stake

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Key property: if sequencer posts incorrect state commitment, any honest challenger can win dispute resolution  $\rightarrow$  no safety violation, and big economic penalty to sequencer.

would expect sequencer to only publish correct state commitments

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- DoS attacks (e.g., if only whitelisted challengers)
- failure of L1 (i.e., not consistent/live/censorship-resistant)
- bribery (i.e., dishonest rollup sequencer pays L1 validators to exclude challengers' L1 txs)

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- rollup users have option to treat rollups txs as finalized earlier, if desired
  - cf., security parameter k in longest-chain consensus

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– in practice, N ≈ 60 and T ≈ 50K (7 days), so N/T ≈ 0.12%