Lecture #23: Proof-of-Stake Blockchain Protocols

COMS 4995-001: The Science of Blockchains URL: https://timroughgarden.org/s25/

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Goals for Lecture #23

- 1. Weighted round-robin.
 - quick and dirty approach to stake-proportional leader selection
- 2. Degrees of permissionlessness.
 - sense in which PoS protocols are "more permissioned" than PoW
- 3. A proof-of-stake Tendermint.
 - consistent and live in partial synchrony under appropriate assumptions
- 4. Slashing.
 - programmatically fight back against a 51%-type attack

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- \rightarrow risk of bribery, coercion, DoS attacks
- also has its benefits (e.g., for tx dissemination)

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- cf., parameterizing by:
 - the number of faulty validators
 - the type of fault (crash vs. Byzantine, etc.)
 - the reliability of the network (sync vs. partial sync vs. async)

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- quasi-permissionless (QP): protocol can also assume that all (non-faulty) list members are actively participating
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- permissioned (Perm): validator set fixed forever when protocol is deployed (e.g., Tendermint)

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- also: no difficulty adjustment algorithm required (stake directly observable)

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- relatively large latency (due to security parameter k)
- much more complex than Nakamoto consensus (see YT videos)
 - e.g., leaders can now equivocate, make multiple proposals per view

Goal: a proof-of-stake protocol that is consistent and (eventually) live in partial synchrony.

Recap: The Partially Synchronous Model

- shared global clock (timesteps=0,1,2,...)
- known upper bound Δ on message delays in normal conditions
- unknown transition time GST ("global stabilization time") from asynchrony to synchrony (i.e., end of attack/outage)
 - protocol must work no matter what GST is

Recall goals:

- consistency, always (even pre-GST/"under attack")
- liveness soon after GST (once "normal conditions" resume)

– FLP → need to give up one of consistency, liveness before GST

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Limitations of Proof-of-Work

- 1. no PoW protocol is consistent in partial synchrony
- 2. even in synchrony, no POW protocol guarantees (deterministic) consistency + liveness

Intuition for (1): catch-22 a la "CAP principle" argument. If validator hears no messages for a long time, can't distinguish between:

- (i) in synchrony, other validators turned off their machines
- (ii) in partial synchrony + pre-GST, all messages delayed

Should the validator ever finalize any additional txs?

- yes → might be in scenario (ii), cause a consistency violation
- no \rightarrow might be in scenario (i), liveness violation (in synchrony) $_{29}$

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Hope: possible in the quasi-permissionless setting.

• recall: offline validators are considered faulty in the QP setting

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Tendermint: Picture of One View



Tendermint: Pseudocode

- at time $4\Delta \cdot v$:
 - each validator i sends its current chain A_i to v's leader ℓ
- at time $4\Delta \cdot v + \Delta$:
 - let A = of the A_i's received, the most recently created one; let B := all not-yet-included (in A) valid txs ℓ knows about
 - ℓ sends proposal (A,B) to all other validators
- at time $4\Delta \cdot v + 2\Delta$:
 - if validator i receives a proposal (A,B) from ℓ with A = A_i or with A more recent than A_i by this time:
 - send "(A,B) is up-to-date" message to all validators
- at time $4\Delta \cdot v + 3\Delta$:
 - if validator i has heard > 2n/3 "up-to-date" msgs for (A,B) by this time (a *read quorum*):
 - package these messages into a quorum certificate (QC), Q
 - send "ack (A,B,Q)" message to all validators and reset $A_i := (A,B,Q)$
- at time $4\Delta \cdot v + 4\Delta$:
 - if validator i has received > 2n/3 "ack (A,B,Q)" messages (a *write quorum*):
 - reset C_i := (A,B,Q) (and also A_i := (A,B,Q), if necessary)

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- add logic to update validator set at epoch boundaries
 - warning: can be hard to get right (without a synchrony assumption)

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In general: can usually (not always) turn a permissioned protocol into a PoS protocol with the same guarantees in the QP setting. 45

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Version #2: programmatic (i.e., in-protocol) slashing.

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 - issue: could have been caused by unreliable network or censoring by other validators, rather than Byzantine behavior

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- design decision: how much to slash for various offenses?

Ongoing debate: in-protocol slashing, or social slashing only?

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 - can always simulate in-protocol slashing, only more options
 - counterpoint: social slashing likely either (i) too hard, won't actually happen when you need it; or (ii) too easy, subject to abuse

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- solution #2: combine Tendermint with some aspects of longestchain consensus (which scales well with # of validators)
- solution #3: use randomly sampled "committees" of validators