Lecture #6: Solving SMR with Byzantine Faults in Partial Synchrony: The Essence of Tendermint

> COMS 4995-001: The Science of Blockchains URL: https://timroughgarden.org/s25/

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Goals for Lecture #6

- 1. The Tendermint protocol.
 - basis of Cosmos and several other blockchain protocols
 - available more or less off-the-shelf to build on
- 2. Analysis of the Tendermint protocol.
 - achieves optimal Byzantine fault-tolerance in partial synchrony
 - similar structure to Paxos/Raft analysis, but several new ideas

State Machine Replication (SMR)

SMR: version of consensus appropriate for a blockchain protocol.

- "state machine" = for us, current state of virtual machine
- "replication" = all validators perform same state transitions
- "clients" submit transactions ("txs") to validators
- each validator maintains an append-only list of finalized txs (a.k.a. "log" or "history")

Goal: a protocol that satisfies consistency and liveness.



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A Road Map to Practical SMR Protocols



Lecture #3: Protocol B solves SMR with crash faults in synchrony.

Lecture #4: Paxos/Raft, optimal crash-fault tolerance in partial synchrony.

Lecture #5: can't achieve >33% Byzantine fault-tolerance in partial synchrony.

Recall: need to assume < n/3 Byzantine validators.

Post-GST Crashes or Pre-GST Delays?





Scenario #2

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Idea #1: every validator signs every message it sends.

- assume all validators know each others public keys (+ IDs + IP addrs)
- called a "public key infrastructure (PKI)" assumption

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- QCs included as metadata alongside blocks

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- all messages annotated with current view number



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- at time $4\Delta \cdot \nu + 2\Delta$:
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- at time $4\Delta \cdot \nu + 3\Delta$:
 - if validator i has heard > 2n/3 "up-to-date" msgs for (A,B) by this time:
 - package these messages into a quorum certificate (QC), Q
 - send "ack (A,B,Q)" message to all validators
 - reset $A_i := (A, B, Q)$

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- at time $4\Delta \cdot v$:
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- at time $4\Delta \cdot v + 3\Delta$:
 - if validator i has heard > 2n/3 "up-to-date" msgs for (A,B) by this time (a read quorum):
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 - send "ack (A,B,Q)" message to all validators and reset A_i := (A,B,Q)
- at time $4\Delta \cdot v + 4\Delta$:
 - if validator i has received > 2n/3 "ack (A,B,Q)" messages (a write quorum):
 - reset C_i := (A,B,Q) (and also A_i := (A,B,Q), if necessary)

Recap: The Partially Synchronous Model

- shared global clock (timesteps=0,1,2,...)
- known upper bound Δ on message delays in normal conditions
- unknown transition time GST ("global stabilization time") from asynchrony to synchrony (i.e., end of attack/outage)
 - protocol must work no matter what GST is

Recall goals:

- consistency, always (even pre-GST/"under attack")
- liveness soon after GST (once "normal conditions" resume)
 FLP → need to give up one of consistency, liveness before GST

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 - consequence: all updates to non-faulty C_i's in views v' > v are to chains that extend A^{*}. [reason: never update without a QC]

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- (1) → simultaneous updates (i.e., in same view) are consistent
- (2) → every update extends all updates from all previous views

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- some non-faulty validator i is in both Q_1 and Q_2
- since i sent an up-to-date message for only one leader proposal (A,B), Q₁ and Q₂ must both be for (A,B)

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In general (by induction on v' > v): for each j in U, A_j is either A^* or a chain+QC created in a view > v (which, inductively, extends A^*).

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Tendermint: Proof of Liveness

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- post-GST \rightarrow all non-faulty validators get (A,B) by $4\Delta \cdot v + 2\Delta$

- by choice of A, all send "(A,B) up-to-date" messages at that time

- post-GST → by time 4Δ · v + Δ, i will receive A_j's from all nonfaulty validators (+ possibly some Byzantine validators)
- let A = most recent of these (i.e., QC from the largest view)
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- post-GST \rightarrow all non-faulty validators get (A,B) by $4\Delta \cdot v + 2\Delta$
 - by choice of A, all send "(A,B) up-to-date" messages at that time
- post-GST → all non-faulty validators get > 2n/3 "(A,B) up-to-date" messages by time 4Δ · v + 3Δ
 - all send "ack (A,B,Q)" messages at that time
- post-GST → all non-faulty validators j get > 2n/3 "ack (A,B,Q)" messages by time 4Δ · v + 4Δ, set C_j := (A,B,Q) [thereby finalizing tx z]