

# Lecture #8: UTXOs and Accounts

COMS 4995-001:  
The Science of Blockchains

URL: <https://timroughgarden.org/s25/>

Tim Roughgarden

# Responsibilities of a Blockchain Protocol

**Consensus:** decide on a sequence (aka “chain”) of blocks.

- note: all validators must agree on this sequence!
- blocks keeping getting added (one-by-one) as long as there are transactions to process
- SMR, Tendermint vs. longest-chain consensus, etc.

# The Consensus Layer

transactions  
(submitted by clients)

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tx1: 1010.....111

tx3: 1110.....000

tx2: 0110.....110

tx4: 0010.....101

blockchain protocol  
(consensus layer)

output log of ordered and  
finalized transactions

tx2

tx3

tx1

tx4

# Responsibilities of a Blockchain Protocol

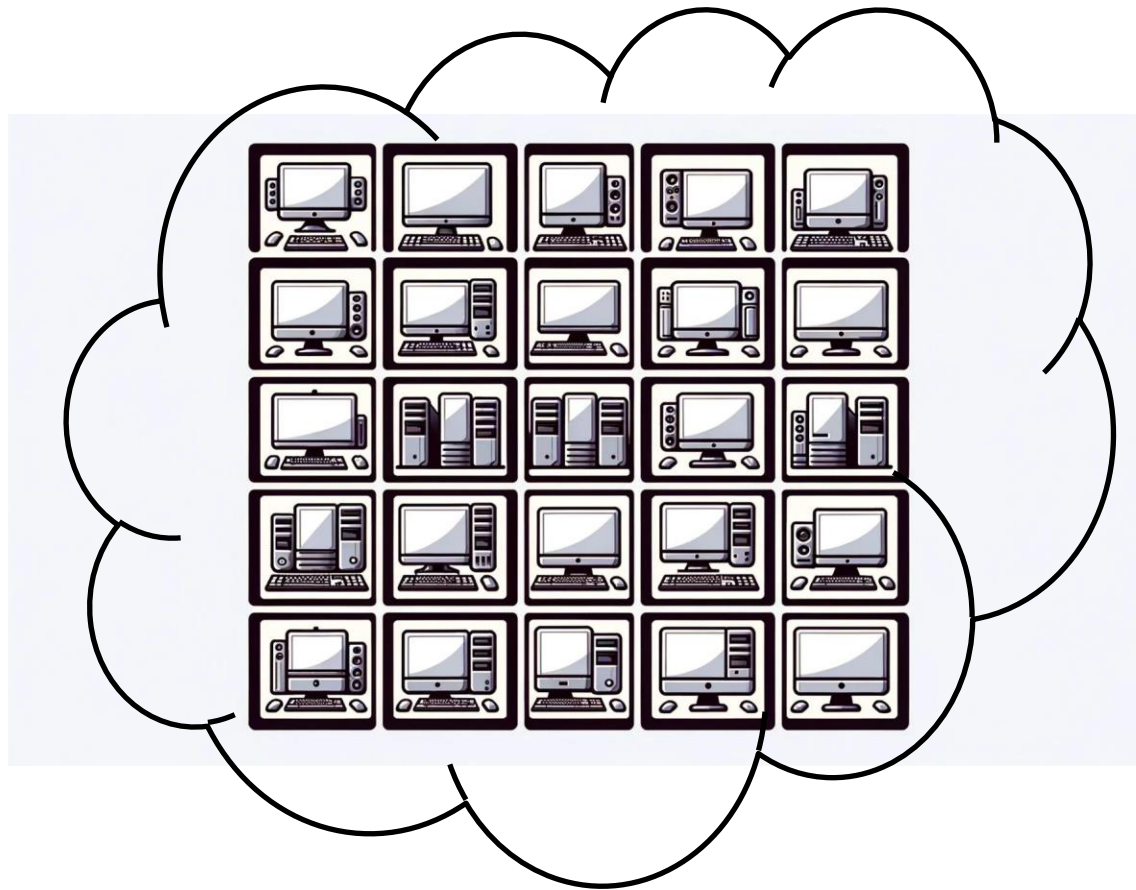
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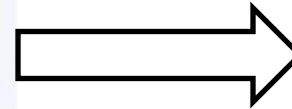
**Execution:** keep state of the virtual machine up-to-date.

- new block added → execute the corresponding snippets of code (do computations, update variable values, etc.)
- subject of this week (concludes Part I of course)

# The Computer in the Sky

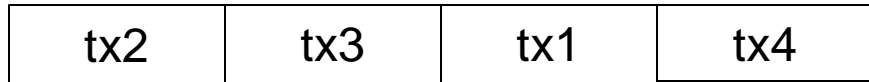


network of physical computers  
+ blockchain protocol



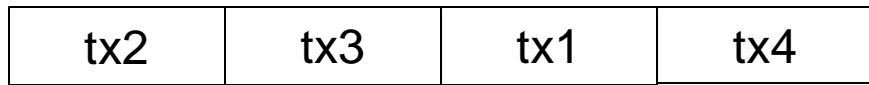
simulated (virtual) computer

# The Execution Layer

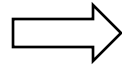


consensus transaction sequence

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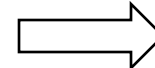
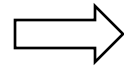


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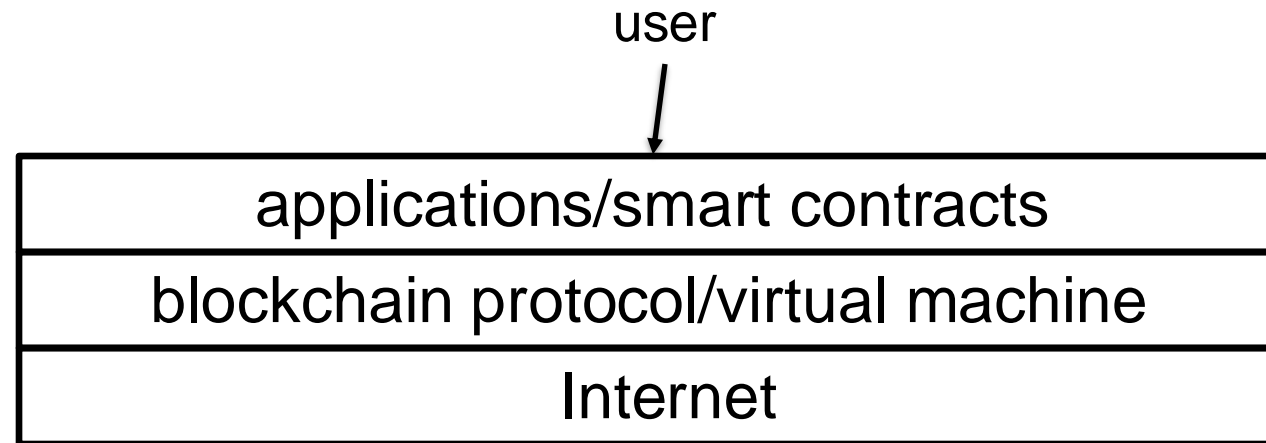
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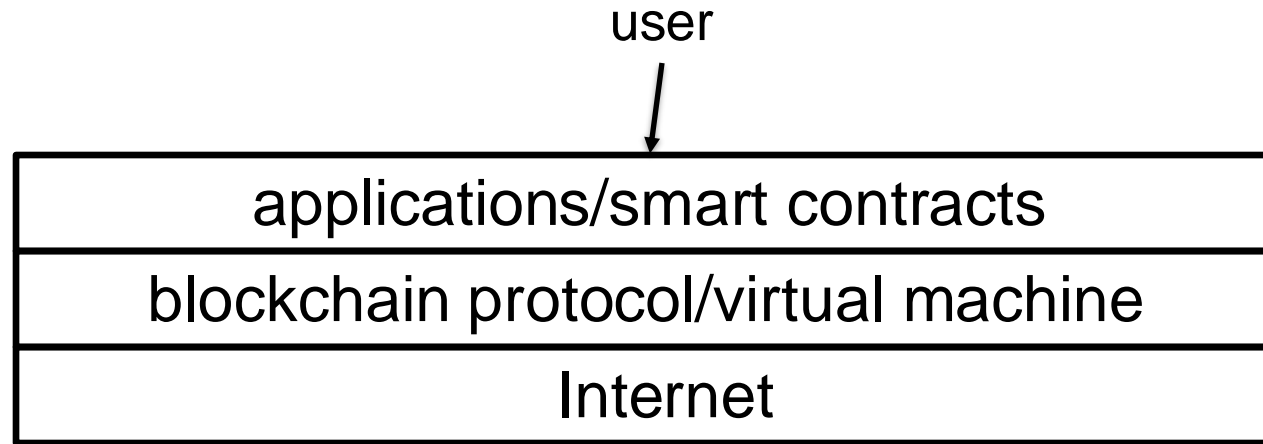
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# Recap: A Cartoon of Web3



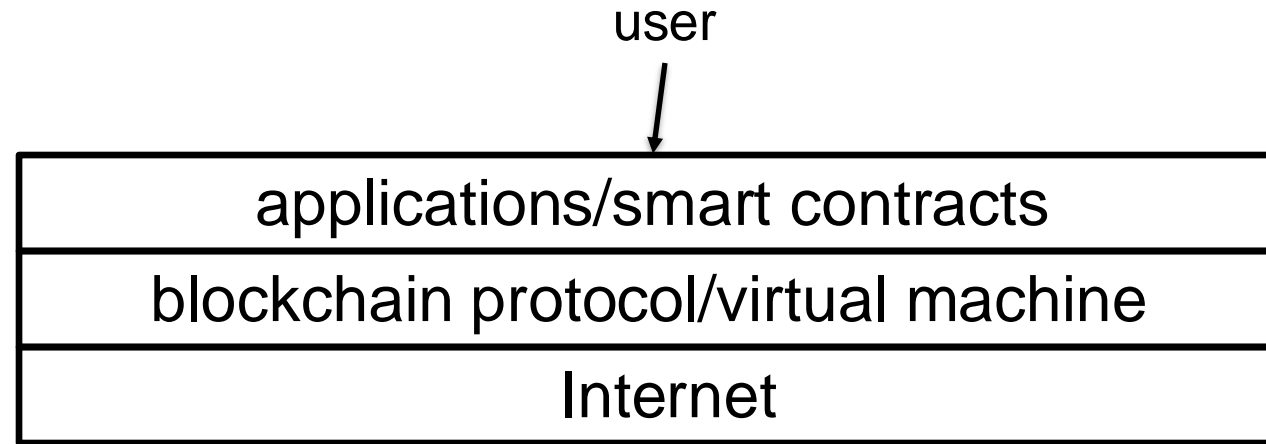
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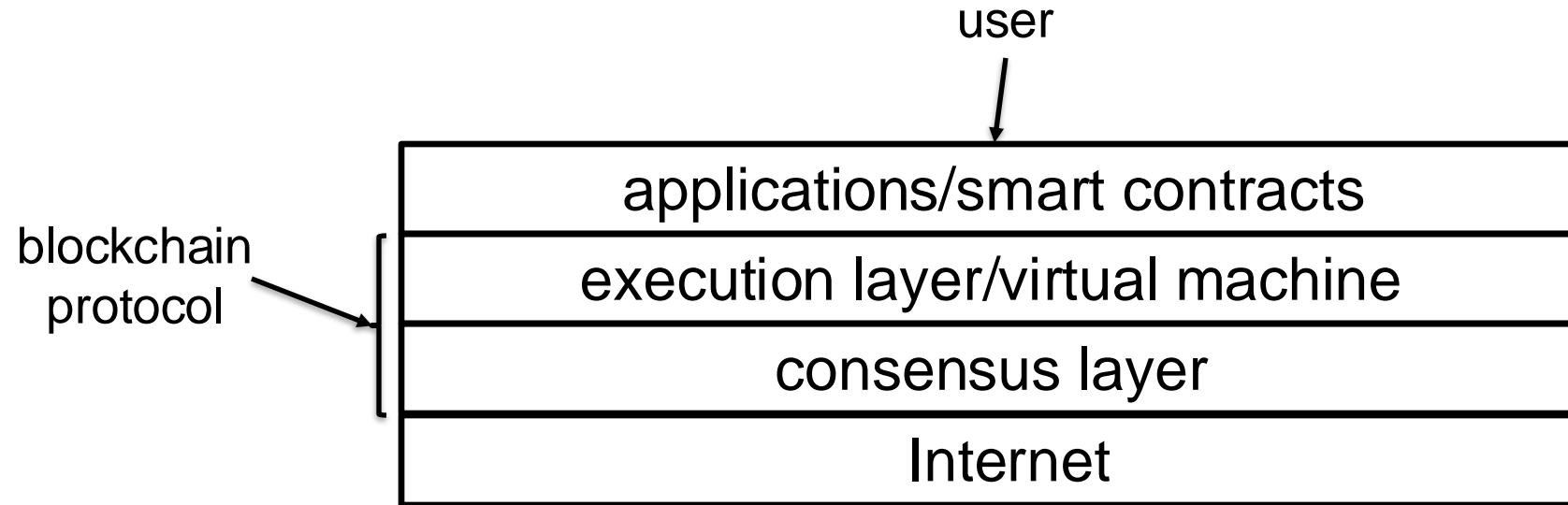
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# A Cartoon of Web3 (Refined)



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# Goals for Lecture #8

1. The UTXO model (used, e.g., in Bitcoin).
  - counterintuitive but elegant VM specialized for payments
2. Measuring the size of a transaction.
  - idea: what resources are required (now and forever) by a transaction?
  - in practice, very tricky!
3. The account-based model (used in Ethereum and Solana).
  - explicit notion of account IDs and balances, programs as accounts
4. Metering computation.

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**Next:** warm-up with deep dive on Bitcoin’s “execution layer.”

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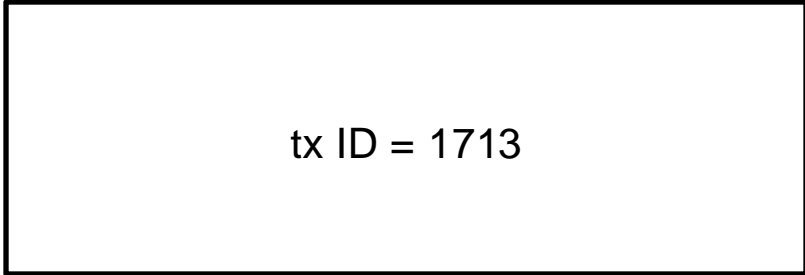
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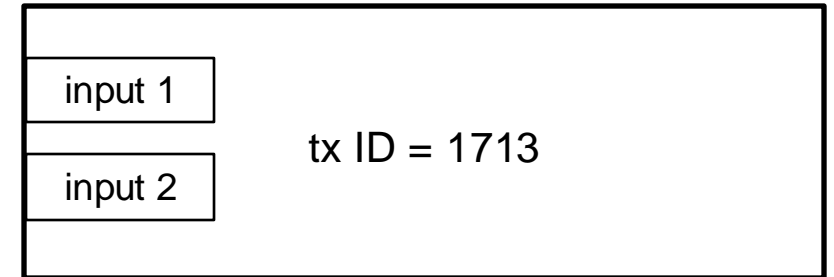


tx ID = 1713

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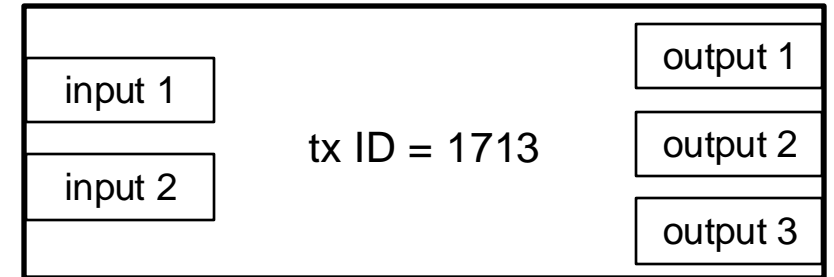
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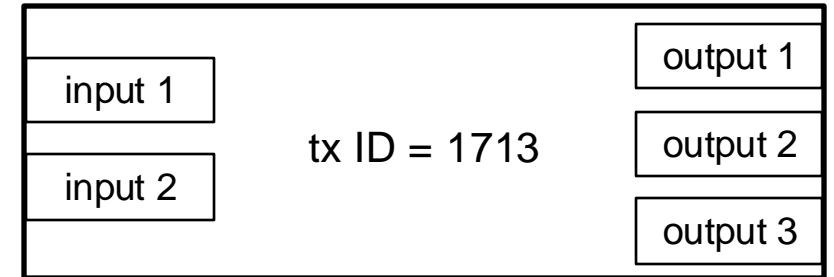
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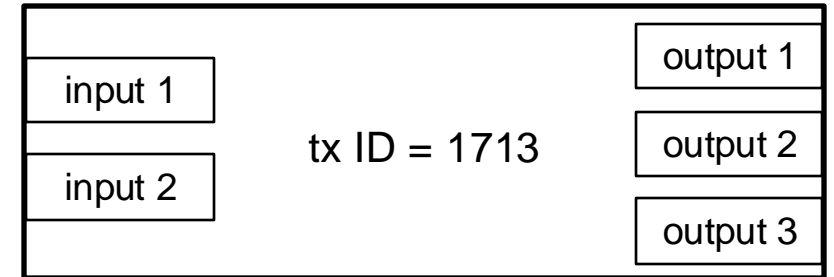
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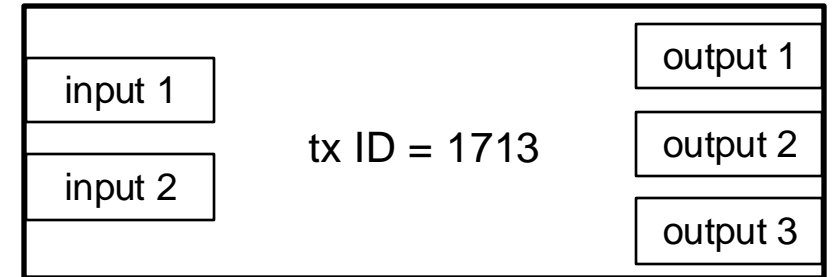
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- format for one input
  - output of some other tx [should be unspent!  $\rightarrow$  “UTXO”]
  - “witness” satisfying output’s spending condition [typically,  $\approx$  a signature]



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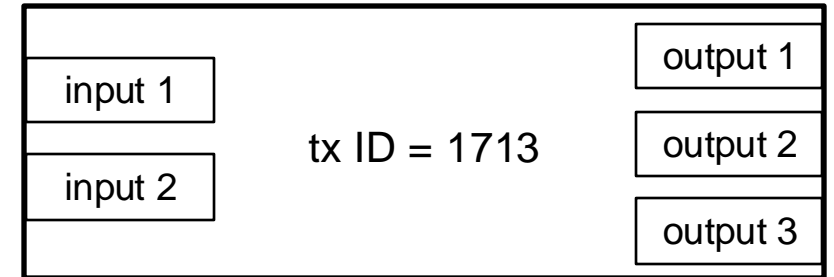


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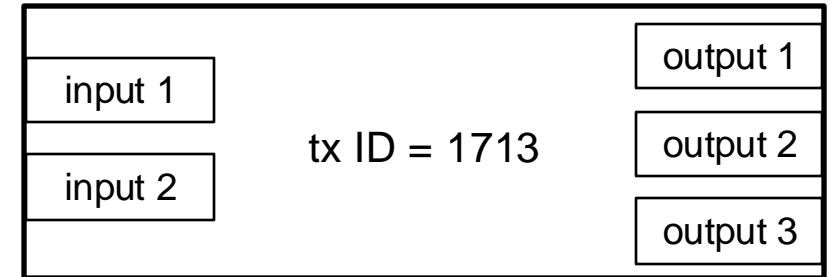
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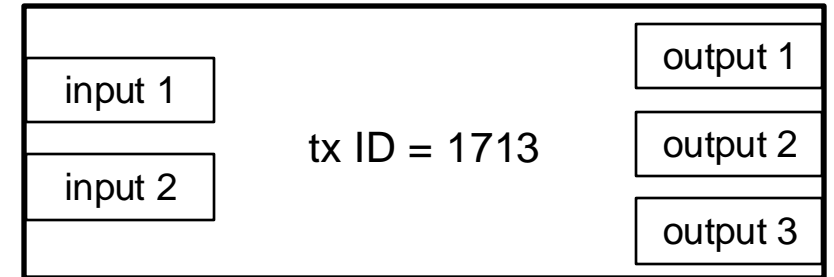
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- for each input, witness satisfies UTXO’s spending conditions

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- canonical implementation = “Bitcoin core”

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**Challenge:** multiple types of resources required:

- resources at the consensus layer (bandwidth)
- resources at the execution layer (computation, memory access)
- resources for long-term storage (at validators or elsewhere)

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**Further challenge:** resource consumption may depend on external-to-protocol factors (e.g., specific client implementation and/or validator architecture).

- in practice, “size” often defined w.r.t. some canonical implementation

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- lowers barrier to participating, but raises barrier to validating
- benefits of innovating vs. benefits of hardening
- led to Bitcoin Cash (fork of Bitcoin with bigger blocks, now irrelevant)

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- **idea:** validator can discard witnesses after checking tx validity
  - “archival nodes” should still keep witness data for posterity



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- **debate:** are these good for Bitcoin?

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**Point:** definition of transaction size can fundamentally affect how a blockchain protocol is used!

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**Example:** in Ethereum, a user account (“EOA”) has no code, only data is a “nonce” [= # of txs sent by account, prevents “replay attacks”].

- all other data on user stored in contracts’ accounts

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- user prepays for gas (part of the tx description)
- run out of gas mid-execution → tx aborted and rolled back