

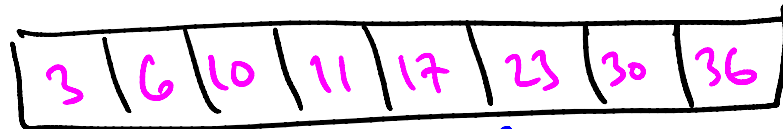


Design and Analysis
of Algorithms I

Data Structures

Balanced Search
Trees: Supported
Operations

Sorted Arrays: Supported Operations



BUT WHAT ABOUT
INSERTIONS + DELETIONS ?
(would take $\theta(n)$ time)

OPERATIONS

SEARCH

SELECT (given order statistic l)

MIN/MAX

PRED/SUCC (given pointer to a key)

RANK (i.e., # of keys less than or equal to
a given value)

OUTPUT IN SORTED ORDER

RUNNING TIME

$\theta(\log(n))$

$O(1)$

$O(1)$

$O(1)$

$O(\log(n))$

$O(n)$

Balanced Search Trees: Supported Operations

Raison d'être : like sorted array + fast (logarithmic) inserts + deletes !

OPERATIONS

SEARCH

SELECT

MIN/MAX

PRED/SUCC

RANK

OUTPUT IN SORTED ORDER

INSERT

DELETE

RUNNING TIME

$\theta(\log(n))$

$O(\log(n))$

$O(\log(n))$

$O(\log(n))$

$O(\log(n))$

$O(n)$

$O(\log(n))$

$O(\log(n))$

Up from
 $O(1)$

new

Also
supported
by hash
tables

Also
supported
by heaps